

Polygons and Area in the Plane

POLYGONS — definition, types, and naming

Polygon

Convex vs. Concave Polygons

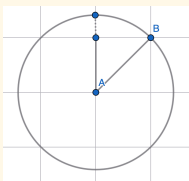
Convex

Concave

Sides	Polygon Name	Sides	Polygon Name
3	Triangle	8	Octagon
4	Quadrilateral	9	Nonagon
5	Pentagon	10	Decagon
6	Hexagon	11	Hendecagon
7	Heptagon	12	Dodecagon
n	n-gon		

PERIMETER WITH SLANTED SIDES

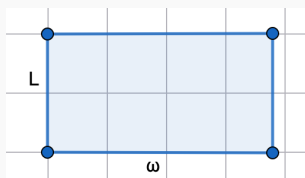
Why Can't We Count Grid Squares for Slanted Sides?



Counting grid squares measures:

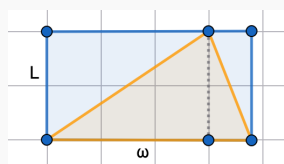
For slanted sides we must use:

Rectangle — $A = l \times w$



Formula: $A = \underline{\hspace{1cm}} \times \underline{\hspace{1cm}}$

Triangle — $A = \frac{1}{2} b \times h$



Formula: $A = \frac{1}{2} \times \underline{\hspace{1cm}} \times \underline{\hspace{1cm}}$

Visual argument

Practice

1. A triangle has vertices at $A(0, 0)$, $B(6, 0)$, and $C(6, 4)$. Find its perimeter.
2. A quadrilateral has vertices at $P(1, 1)$, $Q(5, 1)$, $R(5, 4)$, $S(1, 4)$. Find its area.
3. A triangle has base 8 cm and height 5 cm. Find its area.
4. A polygon has vertices $(0,0)$, $(4,0)$, $(4,3)$, $(2,5)$, $(0,3)$. Classify it by name. Is it convex or concave?